

# MECHANICAL ENGINEERING

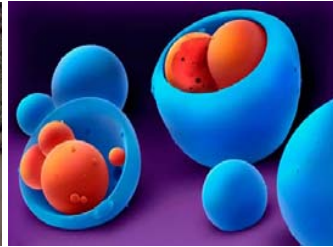
## Numerical Study of Crossflow Enhanced Microfiltration of Oil-in-Water Emulsions

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### Motivation

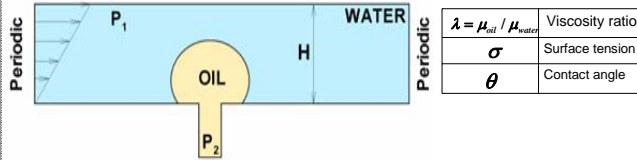


❖ **Microfiltration of Oil-in-Water Emulsions**  
(Oil Spill, Source: <http://bigpicture.ru>)

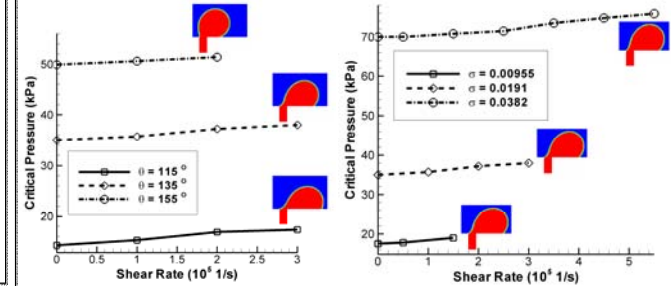


❖ **Controlled Production of Emulsions**  
(Drug delivery using Emulsions)

- Solver: FLUENT.
- Supplemented by: UDF programming (C)
- **3D-simulations** of incompressible Navier-Stokes.
- Interface tracking: **Volume of Fluid (VOF)**.

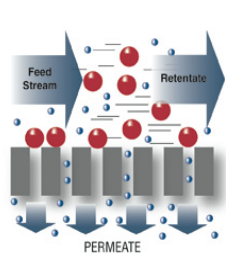


### Results: Effect of Material Parameters

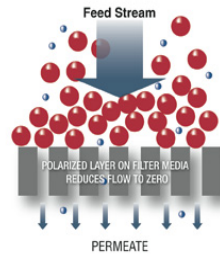


- ❖ Drops with high contact angle and high surface tension have higher critical pressure.
- ❖ Drops of high contact angle and low surface tension break more easily.

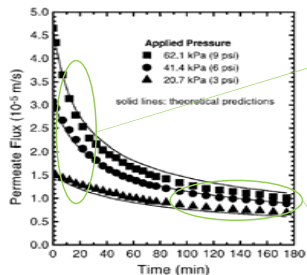
### Types of Microfiltration and Typical Issues



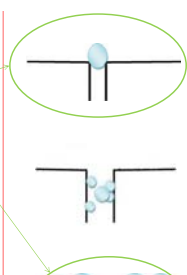
Crossflow Filtration



Dead-end Filtration



❖ Flux decline in crossflow microfiltration of a silica suspension.

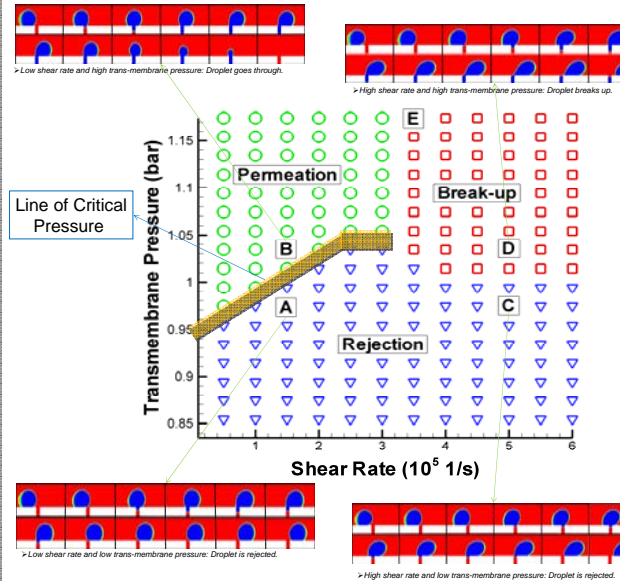


➤ **Complete Blocking:**  
Happens at the initial stages of filtration. A droplet blocks the pore completely.

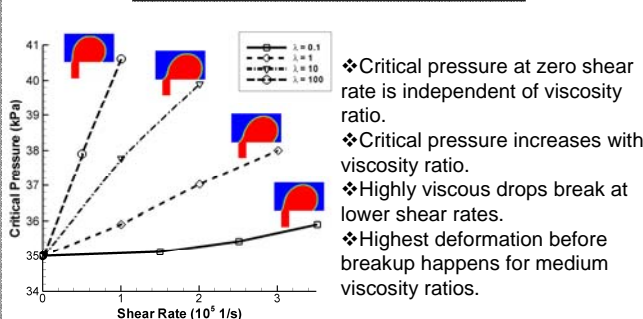
➤ **Standard blocking:**  
Deposition of drops inside the pore.

➤ **Cake Formation:**  
Happens at the final stages of filtration. A layer of drops forms on the surface.

### Results: Effect of Transmembrane Pressure and Shear Rate

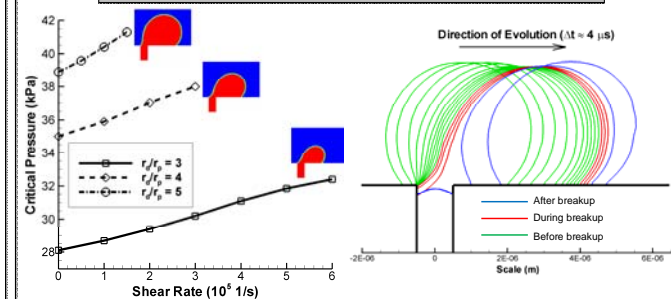


### Results: Effect of Viscosity Ratio



- ❖ Critical pressure at zero shear rate is independent of viscosity ratio.
- ❖ Critical pressure increases with viscosity ratio.
- ❖ Highly viscous drops break at lower shear rates.
- ❖ Highest deformation before breakup happens for medium viscosity ratios.

### Results: Drop Dynamics and Effect of Drop Size



- ❖ Larger drops break more locally. Small drops break through necking.
- ❖ Larger drops break more easily than smaller drops.
- ❖ Drop breakup time scale is small compared to flow time scale.

### Important Conclusions

- ✓ Behavior of a single droplet on a pore in crossflow microfiltration is one of the following: Permeation, Rejection, Breakup.
- ✓ Critical pressure for crossflow microfiltration increases with shear rate, viscosity ratio, surface tension coefficient, and drop size.
- ✓ Increasing viscosity ratio, contact angle, and size of the drop increases chance of breakup.
- ✓ Increasing the surface tension coefficient decreases chance of breakup.

### References

1. "Microfiltration of Water-in-Oil Emulsions", F.F. Nazzari and M.R. Wiesner, Water Environment Research, Vol. 68, No 7 (1996).
2. "Kinetics of Permeate Flux Decline in Crossflow Membrane Filtration of Colloidal Suspensions", S. Hong, R.S. Faibish, and M. Elimelech, Journal of Colloid and Interface Science 196, 267-277 (1997).
3. "An Experimental Investigation of Drop Deformation and Breakup in Steady Two-dimensional Linear Flows", B.J. Bentley and L.G. Leal, Journal of Fluid Mechanics, 167, 241-283 (1986).

Pressure jump across static interface:  
**Young-Laplace Equation**

### Theory and Numerical Method

$$\Delta P = \gamma \cos \theta \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$

$$\Delta P(P_1 - P_3) = (P_1 - P_2) + (P_2 - P_3)$$

$$\Delta P = \gamma \cos \theta \left( \frac{1}{R_1} + \frac{1}{R_2} \right)$$